

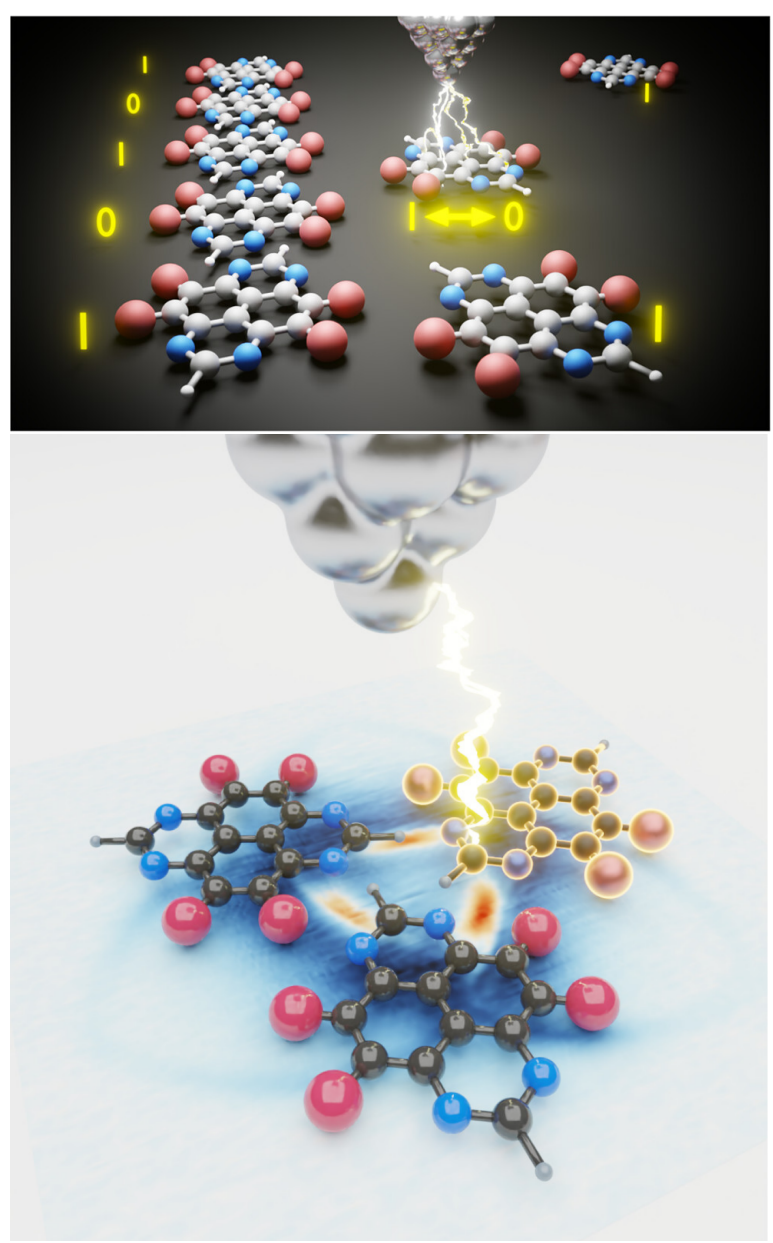


Individual Assembly of Radical Molecules on a Superconductor

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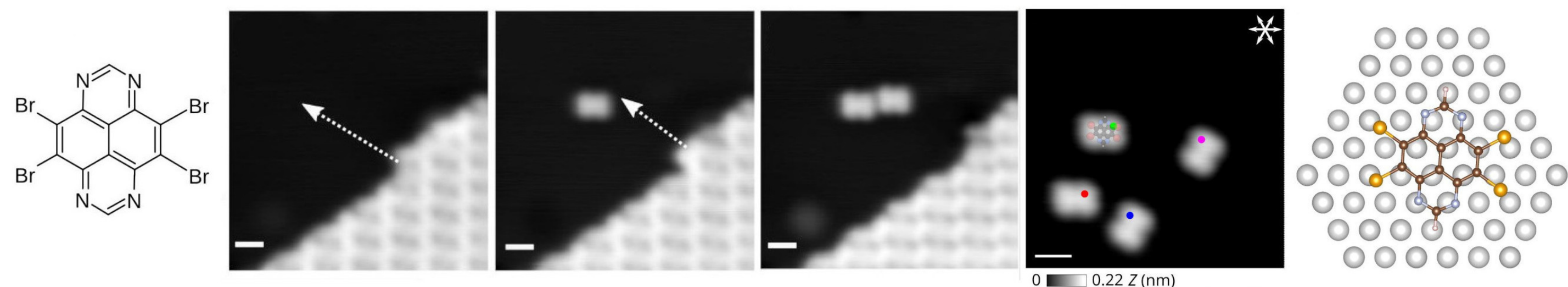
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Motivation



- Magnetic molecules on a superconductor:** tunable platforms to study the interplay of electronic correlations, quantum tunneling, magnetism, bound states, topology, entanglement and more.
- Superconducting molecular spintronics:** nanoscale devices that are easy to manipulate, enable low-energy data storage and computing, and can serve as building blocks for logic gates.
- Quantum-dot cellular automata (QCA):** a transistor-free nanotechnology for ultra-high-density, low-power computing in which binary information is encoded in charge configurations rather than current.

TBTAP molecule on a superconducting surface



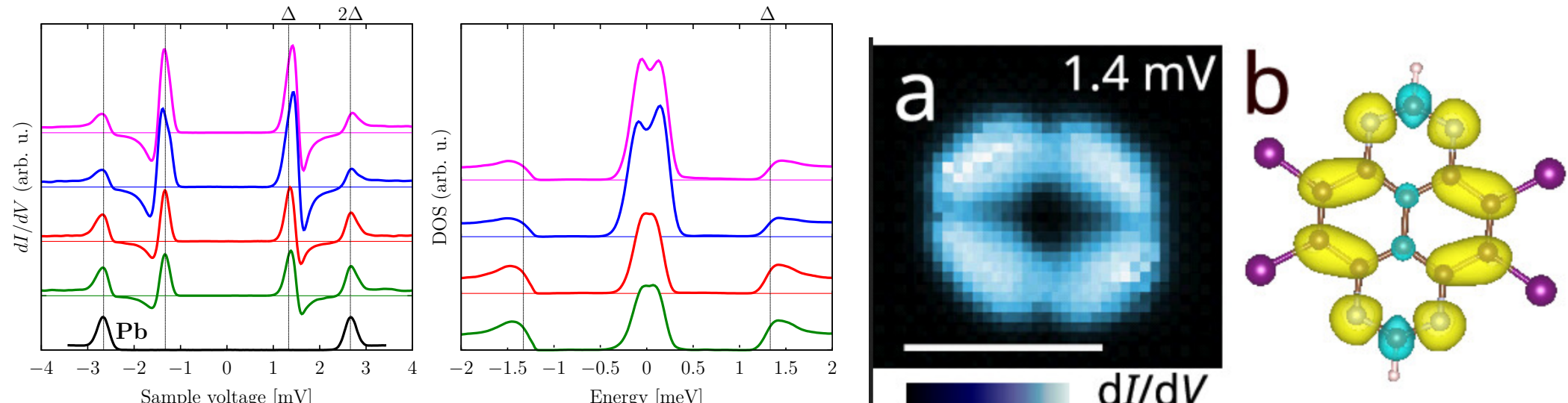
Individual molecules were removed from the island by lateral manipulation (pulling with the scanning tip).

4,5,9,10-tetrabromo-1,3,6,8-tetraazapyrene (TBTAP):

- Acceptor tetraazapyrene backbone decorated with four bromine atoms; **metal-free**.
- Isolated molecule: TBTAP^{•−} radical with a **spin-1/2** ground state on both Pb(111) and Ag(111) [1].
- Forms a densely packed supramolecular network when sublimed onto a Pb(111) surface.
- Stripes of charged (spin-1/2) and neutral (spin-0) molecules [2].

Tunneling spectra:

- Measured at $T_{\text{exp}} = 1\text{ K}$ (2.6 K for the trimer) using a superconducting Pb tip to enhance resolution.
- Deconvolution performed via the **maximum-entropy method** (modified *ana.cont* package [3]).

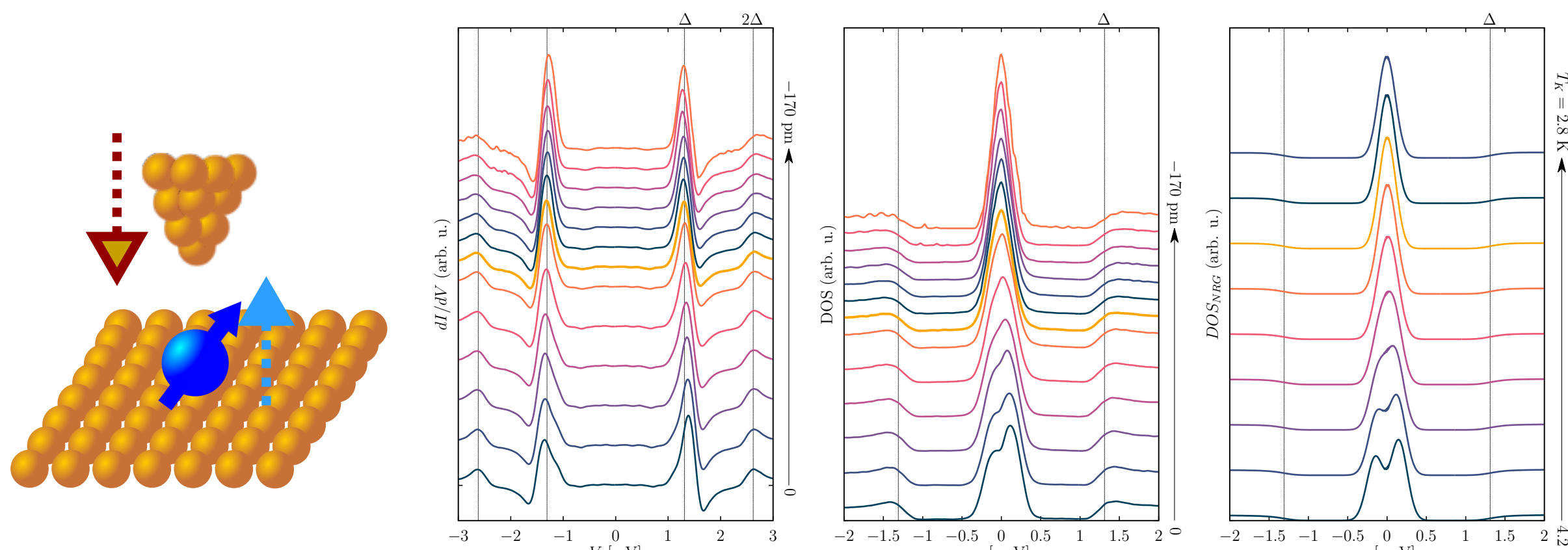


- Results show a gap $\Delta \approx 1.3\text{ meV}$ and a single pair of **Yu-Shiba-Rusinov** (YSR) states along the molecular backbone, very close to zero energy.
- This indicates that TBTAP on Pb(111) is **naturally close to a singlet-doublet impurity quantum phase transition** (QPT).
- The Coulomb interaction $U \approx 200\text{ meV}$, obtained from the gap measurement, places the system in the Kondo regime with $k_B T_K = 0.29\sqrt{\Gamma U \exp[-\pi U/(8\Gamma)]}$.
- For $U \gg \Delta$, one can use $k_B T_K^C \approx \Delta/(e^{5/3} - 1) \approx 0.23\Delta$ [4], giving $T_K^C = 3.5\text{ K}$.

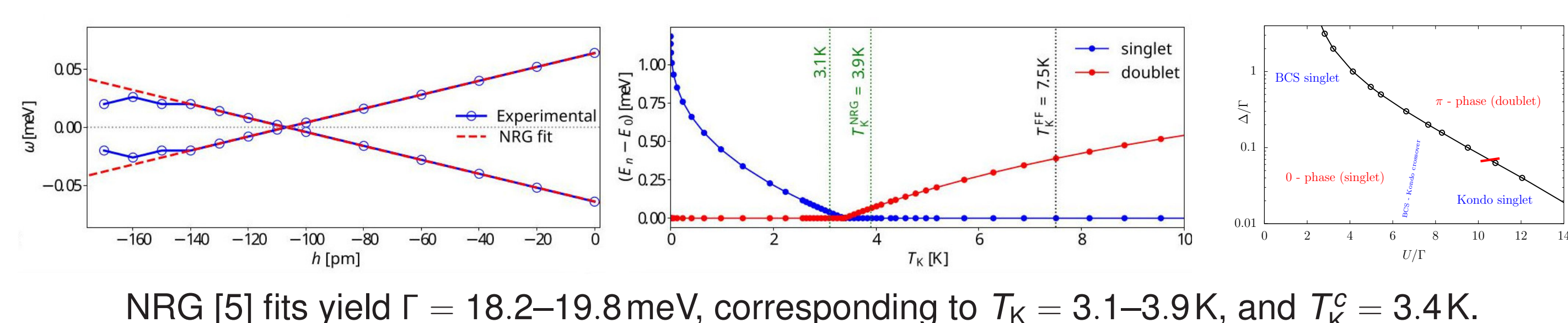
Triggering the QPT

Tunneling spectra at different tip heights:

- Decreasing the STM tip height reduces the coupling to the substrate, Γ_s , by lifting the molecule via attractive interaction.
- YSR states cross at the Fermi energy at $h \approx -110\text{ pm}$ —a hallmark of a QPT.



Extracting T_K^C from the YSR evolution



NRG [5] fits yield $\Gamma = 18.2\text{--}19.8\text{ meV}$, corresponding to $T_K = 3.1\text{--}3.9\text{ K}$, and $T_K^C = 3.4\text{ K}$.

References and Acknowledgments

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[3] J. Kaufmann and K. Held, *Comput. Phys. Commun.* **282**, 108519 (2023); [4] A. Kadlecová *et al.*, *Phys. Rev. Appl.* **11**, 044094 (2019); [5] R. Žitko, NRG Ljubljana (8f90ac4), Zenodo (2021);
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We acknowledge support from the Czech Science Foundation (project No. 23-05263K) and EU COST action CA24109 **QOpen**.



Model: Superconducting Anderson-Hubbard Impurity Model

An ensemble of N_d interacting impurities:

$$\mathcal{H}^{\text{en}} = \sum_{j=1}^{N_d} \sum_{\sigma} \epsilon_j n_{j\sigma} + \sum_{j=1}^{N_d} U_j n_{j\uparrow} n_{j\downarrow} - \sum_{i=1}^{N_d} \sum_{j=1}^{N_d} \sum_{\sigma} t_{ij} d_{i\sigma}^{\dagger} d_{j\sigma} + \sum_{i=1}^{N_d-1} \sum_{j>i}^{N_d} W_{ij} (n_{i\uparrow} + n_{i\downarrow}) (n_{j\uparrow} + n_{j\downarrow})$$

N_l superconducting leads (tip and surface):

$$\mathcal{H}_l^{\text{le}} = \sum_{\mathbf{k}\sigma} \epsilon_{l\mathbf{k}} c_{l\mathbf{k}\sigma}^{\dagger} c_{l\mathbf{k}\sigma} - \Delta \sum_{\mathbf{k}} \left(e^{i\varphi_l} c_{l\mathbf{k}\uparrow}^{\dagger} c_{l,-\mathbf{k}\downarrow}^{\dagger} + \text{H.c.} \right) + \sum_{\mathbf{k}\sigma} \left(V_{j,l\mathbf{k}} c_{l\mathbf{k}\sigma}^{\dagger} d_{j\sigma} + \text{H.c.} \right)$$

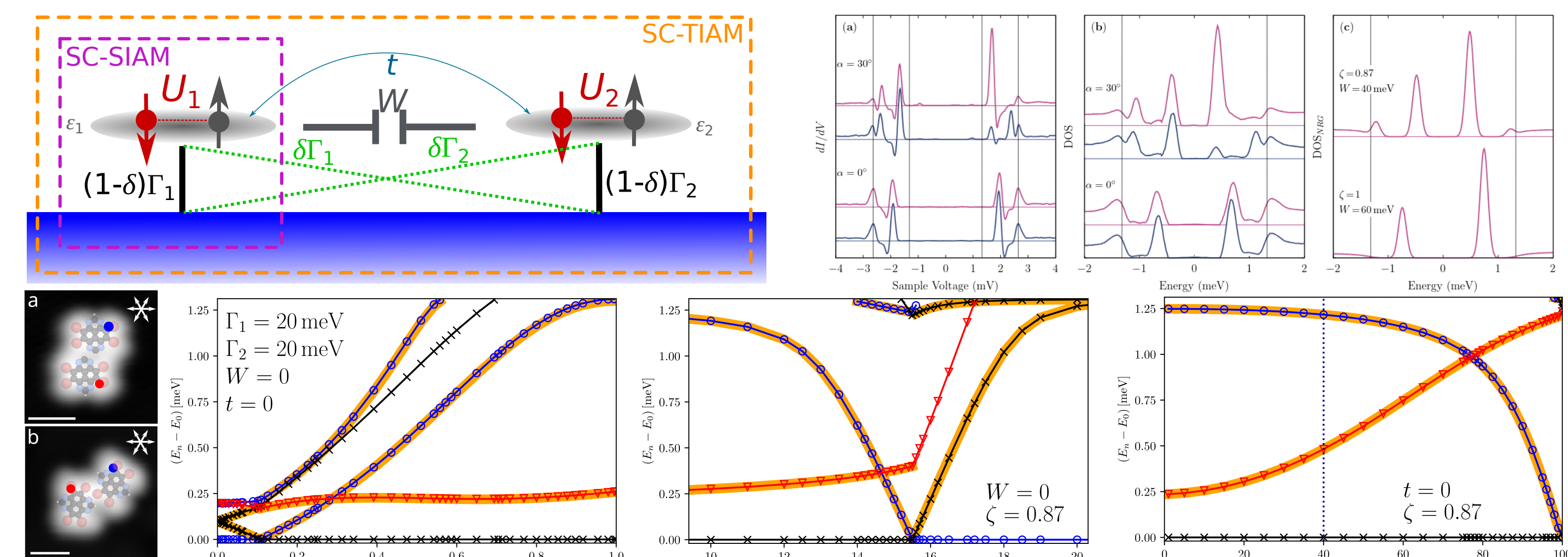
Local and non-local tunneling rates:

$$\Gamma_{j,l}(E) = \pi \sum_{\mathbf{k}} |V_{j,l\mathbf{k}}|^2 \delta(E - \epsilon_{\mathbf{k}}) = \Gamma_{jl}, \quad \Gamma_{ij,l}(E) = \pi \sum_{\mathbf{k}} V_{i,l\mathbf{k}}^* V_{j,l\mathbf{k}} \delta(E - \epsilon_{\mathbf{k}}) = \zeta \sqrt{\Gamma_{il} \Gamma_{jl}}.$$

ζ parametrizes the distance: $\zeta = 0$ (large distance), $\zeta = 1$ (local, two-level impurity).

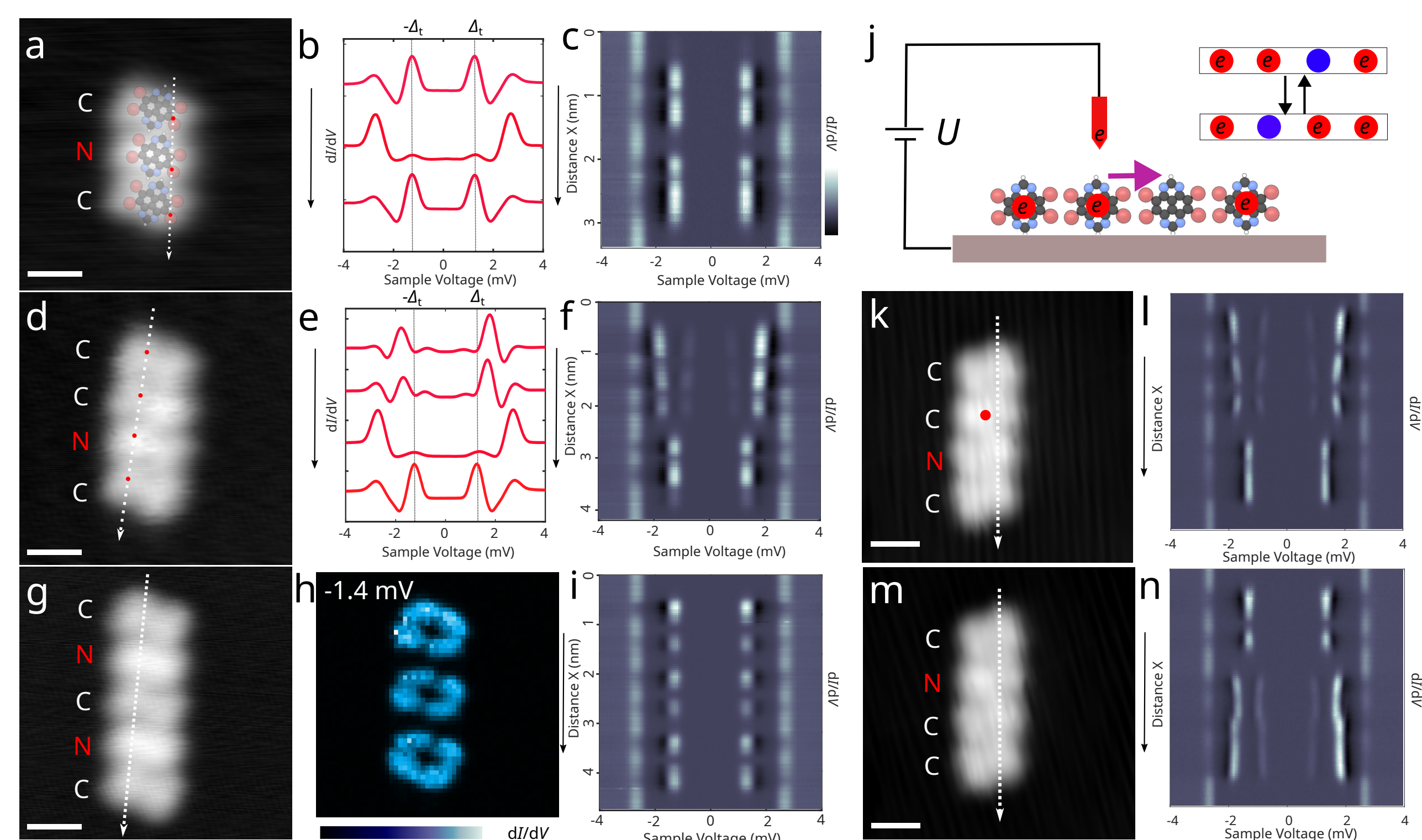
Short molecular chains

Two types of dimers engineered via lateral manipulation:



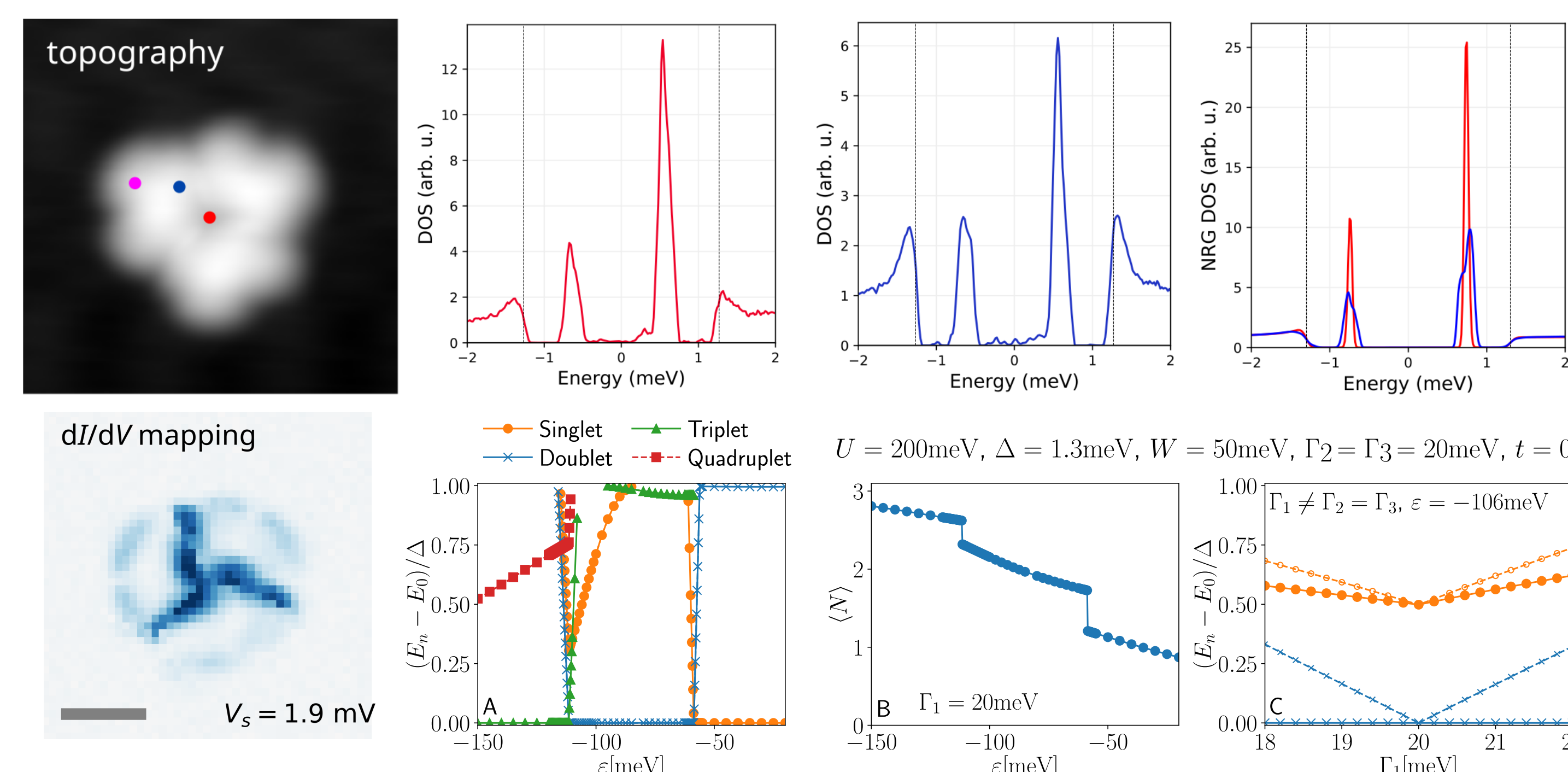
- Two pairs of YSR states for $\alpha = 30^\circ$ and a single pair for $\alpha = 0^\circ$.
- Large distance (small ζ): singlet with YSR states near the Fermi energy—like an isolated molecule.
- Singlet-doublet QPT at $\zeta \sim 0.1$; three, two, and finally one pair of YSR states in the doublet phase.
- By fine-tuning ζ and W , we reproduce the experimental YSR positions in both cases; the **ground state is a doublet in both**.
- We observe an **effective ferromagnetic coupling** in the doublet phase.

Chains of 3, 4, and 5 molecules (same orientation with respect to the surface):



- Chains of odd length show a periodic arrangement of charged and neutral molecules.
- Molecules at the ends are always charged.
- The tetramer is frustrated: a dimer forms at one end.
- It can be switched between the two states using an STM tip, demonstrating information storage.

Trimer in a triangular arrangement



- NRG predicts approximately **two electrons** on the trimer and a **doublet** ground state due to sizable W , consistent with Pauli master-equation (PME) calculations.
- The experimental YSR states are split by $\approx 0.1\text{ meV}$; this is consistent with small differences in the Γ values.
- We develop an effective model describing the influence of molecular distance on YSR [6].